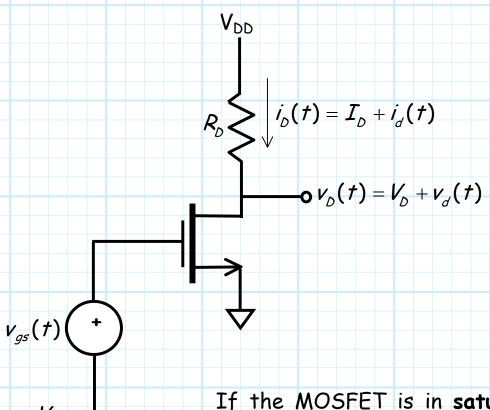
Small-Signal Response of MOSFET Circuits

Consider this circuit, which has both a **DC** and an AC **small-signal** source. As a result, each voltage and current in the circuit has **both** a DC and small-signal component.



If the MOSFET is in saturation, then the total drain current is:

$$i_{D} = K (v_{GS} - V_{t})^{2}$$

$$= K (V_{GS} + v_{gS} - V_{t})^{2}$$

$$= K (V_{GS} - V_{t})^{2} + 2K (V_{GS} - V_{t}) v_{gS} + K v_{gS}^{2}$$

Jim Stiles The Univ. of Kansas Dept. of EECS

By looking at this equation, we find that the **third** term is **small** in comparison to the second **if**:

$$V_{gs} \ll 2(V_{GS} - V_{t})$$

We call this equation the **small-signal** condition. For this case, we find that the drain current is:

$$i_{D}(t) = I_{D} + i_{d}(t)$$

$$\approx K \left(V_{GS} - V_{t}\right)^{2} + 2K \left(V_{GS} - V_{t}\right) V_{gS}(t)$$

Thus, it is evident that the DC equation is:

$$I_D = K (V_{GS} - V_t)^2$$

while the small signal equation is:

$$i_{d}(t) = 2K(V_{GS} - V_{t})v_{gS}(t)$$

Thus, we can define the MOSFET transconductance as:

$$g_m \doteq \frac{i_d}{v_{gs}} = 2K \left(V_{GS} - V_t \right)$$

Note this small-signal parameter g_m can likewise be **derived** from a small-signal analysis of the drain current:

$$i_{d}(t) = \frac{d i_{D}}{d v_{GS}} \bigg|_{v_{GS} = V_{GS}} v_{gs}(t)$$

$$= 2K (v_{GS} - V_{t}) \bigg|_{v_{GS} = V_{GS}} v_{gs}(t)$$

$$= 2K (V_{GS} - V_{t}) v_{gs}(t)$$

$$= g_{m} v_{as}(t)$$

The MOSFET transconductance relates a small **change** in v_{es} to a small **change** in drain current i_D . This change is completely dependent on the **DC** bias point of the MOSFET, V_{es} and I_D .

We can likewise determine the small signal voltage $v_{ds}(t)$. Writing the KVL for the drain-source leg, we find:

$$V_{DD} - R_D i_D = V_{DS}$$

$$V_{DD} - R_D (I_D + i_d) = V_{DS} + V_{dS}$$

$$V_{DD} - R_D I_D - R_D i_d = V_{DS} + V_{dS}$$

The **DC** equation is therefore:

$$V_{DD} - R_D I_D = V_{DS}$$

while the small-signal equation is:

$$-R_{D} i_{d}(t) = V_{ds}(t)$$

Since $i_d(t) = g_m v_{gs}(t)$, we find that the small-signal voltage $v_{ds}(t)$ is related to $v_{gs}(t)$ as:

$$v_{ds}(t) = -R_D i_d(t)$$

$$= -R_D g_m v_{qs}(t)$$

or:

$$\frac{v_{ds}(t)}{v_{gs}(t)} = -R_D g_m$$

Thus, if $R_D g_m \gg 1$, we have small-signal voltage gain.